## Crib 5

written by Alvin Wan . alvinwan.com/cs70

Monday, September 12, 2016

The crib sheet contains cheat-sheet worthy information but is not a substitute for lectures or for reading the notes. It also contains pointers and common mistakes.

## 1 Definition

- In a $\bmod p$ universe, only the values $\{0,1, \ldots p-1\}$ exist. This means no negative numbers or fractions exist.


## 2 Multiplicative Inverse

- The multiplicative inverse of $n$ in $\bmod p\left(\right.$ or, for short, $\left.n^{-1} \bmod p\right)$ is defined so that $n n^{-1}=1 \bmod p$. (Say $p=5$ and $n=3$, then $3\left(3^{-1}\right)=1$ $\bmod 5$. We can see that $3^{-1}=2 \bmod 5$, as $3(2)=6=1 \bmod 5$. We will find an algorithm that computes the multiplicative inverse in the next lecture.)
- The multiplicative inverse of $n$ in $\bmod p$ exists if and only if $n$ is co-prime with $p$. i.e., $n$ and $p$ do not share any common factors greater than 1 .
- Even if $n$ and $p$ are not co-prime, the equation may still have a solution. For example, $2 x=4 \bmod 6$ has a solution, even though 2 is not co-prime with 6 . (Of course, it is easy to see that $x=2$ works.)

